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Structural and Optical Studies of Ho³⁺/yb³⁺ Co-Doped TiO₂ Nanoparticles in Silica Glass

Research Article

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Abstract. The TiO_2 nanoparticles doped with Ho^{3+} and Yb^{3+} ions were synthesized by sol gel method. The structure of the samples were characterized by XRD, TEM and by thermo gravimetric analysis. The average particle size of the TiO_2 range from 7-10 nm (in diameter). The result obtained from TEM, XRD studies indicate that the rare earth ions were positioned in low phonon glass. The photoluminescence (PL) and upconversion (UC) properties of Ho^{3+} in various concentrations of TiO_2 nanoparticles have been investigated. The PL and UC luminescence depends on particle size and crystal structure and we also observed that the emission of Ho^{3+} in silica xerogel was significantly depends on the amount of TiO_2 nanoparticles.

Keywords. Up conversion; Radiative; Quantum efficiency; TiO_2 nanoparticles; Photoluminescence **PACS.** 78.66Jg

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1. Introduction

Luminescent properties of rare-earth embedded in several metal and semiconductor (SC) nanoparticles (NPs) are used because of their many technological applications. Recently, rare earth (RE) ions doped semiconductor nanoparticles have attracted extensive attention due to their unique optical properties and perspective applications in optoelectronics devices and flat panel displays [1–4]. The luminescence property of RE ions in nanocrystals depends critically on their locations in the host. Since the f-orbital is strongly shielded from the outside ligand, the

positions of the spectral lines vary only slightly with the environment. However, their intensities are strongly dependent on the host in which the RE ion is embedded [5]. In general, the RE emission in glassy matrix is strongly dependent on crystal field's effects, local environment, phonon energy and refractive index where the ion is situated [6]. Silicate glasses which are the most chemically and mechanically stable and also more easily fabricated into various shapes and size. The strong luminescence properties can be realized in the glasses with lower phonon energies. So it is difficult to observe in silicate glasses which posses higher phonon energies. Therefore design of SCNPs doped silica glasses are target at present. Preparing nanoscale host materials can change the physical properties of the host which affects the luminescence and dynamics of optically active dopants. High quality nanocrystalline TiO₂ nanoparticles glass of anatase phase were prepared by using sol-gel techniques. Among the RE ions, Ho³⁺ has been recognized as one of the most efficient RE ions for obtaining laser emission due to its numerous radiative emissions in the visible and IR region. Ho³⁺ ions has been extensively studied in various tellurite glasses and ceramics [7,8] Several transitions are of special interest, the ${}^5I_7 \rightarrow {}^5I_8$ emission near 2 μ m is of particular interest because of its use in eye safe systems and medical applications. The blue, green and red up conversion transitions are very important for lighting applications.

In this work, we report the preparation of silica xerogel doped with $\mathrm{Ho^{3+}}$ ions and $\mathrm{TiO_2}$ nanoparticles by sol gel techniques. Structural and luminescent properties of $\mathrm{Ho^{3+}}$ codoped with $\mathrm{Yb^{3+}}$ in $\mathrm{TiO_2\text{-}SiO_2}$ nanoparticles were investigated.

2. Experimental

2.1 Preparation of Er³+/yb³+ ions Doped Titania Samples

A facile sol-gel method was introduced to prepare titania (TiO_2) nanoparticles [6]. The titania sol prepared using the standard procedure starting with high-purity reagents such as titanium isopropoxide (TIPO), isoproponol and HNO₃. Ultra-cleaned glass slides were then dip-coated in this sol and kept overnight for drying at room temperature. The dried film was then heated at 60 °C, at which the films became porous. The thickness of the film was about 54 μ m. in the next step the titania sol was hydrolyzed by adding it drop by drop to an appropriate quantity of distilled water under vigorous stirring. The whole volume was then heated to 60°C for better crystallization of TiO₂ nanoparticles. Appropriate amount of tetraethyle orthosilicate (TEOS) was partially hydrolyzed in mixture of methanol, distilled water, dimethyleformamide (DMF), and HNO₃ by starring the solution for 30 min. To this partially hydrolyzed TEOS, required amount of TIOP was added and stirred for an hour. In this process, the mixing volume of the precursors was so maintained that the SiO₂/TiO₂ ratio becomes 95:5. Finally, dissolved Ho₂O₃ and yb₂O₃ in HNO₃ and stirred for an hour. In this particular molar concentration was added to it and the whole solution was stirred for another half an hour. The resulting sol was poured into small plastic molds for gelation at room temperature (22 °C). In this method, TiO₂ and SiO₂ interacted chemically, i.e., Ti-O-Si linkages were formed.

2.2 Characterization Techniques

The TGA/DTA of the prepared samples was done through a Perkin-Elmer (model: pyris Diamond). During TGA/DTA, the samples were heated from 40 °C to 800 °C at heating rate of 10 °C/min. The X-ray diffraction (XRD) of the sample was recorded using a Philip PW1710 X-ray diffractometer. The transmission electron microscopic (TEM) images were obtained through a using a JEM-2100 transmission electron microscope with recording voltage of 200KV. The optical absorption, Photoluminescence and up conversion spectra were measured at room temperature using iHR 320 imaging spectrometer (Horiba Jobin Yvon) with a 450 xenon (370 nm) and 980 nm diode laser.

3. Result and Discussion

3.1 TGA/DTA

The TGA/DTA studies were performed in order to determine the burn-off temperature of the templating agent, and also the final weight fraction of titanium dioxide. The TGA/DTA results are shown in Figure 1. An endothermic peak is observed at 89 °C in the DTA thermogram, which results from desorption of physically absorbed water and residual solvents. A large exothermic peak appears at around 211 °C, which is in the range of significant weight loss, as evident from the corresponding TGA. This exothermic peak can be attributed to the near complete combustion of organic compounds such as alkyl groups remaining in the solids. At approximately 275 °C, a small exothermic peak is observed, which can be assigned to the carbonization of remaining organic residues. TGA of the sample reveals that the weight loss below 127 °C is 13.35% and between 180 °C and 215 °C the weight loss is 50.16%. The weight loss could be attributed to the carbonization or the combustion of organic compounds.

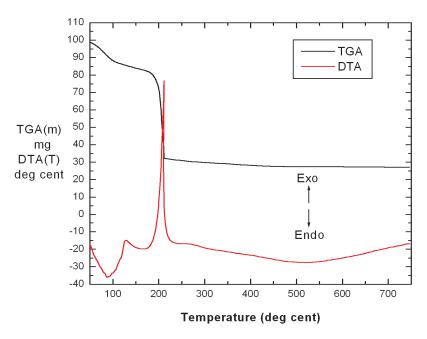


Figure 1. TGA/DTA of TiO₂-SiO₂

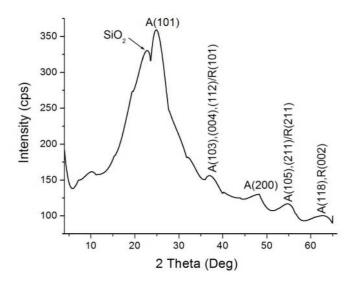


Figure 2. XRD of TiO_2 - SiO_2

3.2 X-ray diffraction

The powder XRD patterns of the Ho³⁺ TiO₂-SiO₂ heated to 800 °C is shown in Figure 2. Two strong and relatively broad peaks can be seen at $2\theta = 6.246$ ° and 18.836 °, which can be assigned as due to Si_xO₂ (0 < x < 1). It is because of the fact that two peaks: one at $2\theta = 6.306$ ° and the other at $2\theta = 18.995$ ° have already been reported in the case of Si_{0.98}O₂ (JCPDS card no.: 81-2467). The small XRD peaks appearing at 25.499 ° and 54.013 ° indicate the presence anatase TiO₂ phases A (101) and A (105) respectively. The TiO₂ crystallite size calculated with the help of Debye-Scherrer formula, $t = 0.9\lambda/B\cos\theta$, where λ is the wavelength of x-ray radiation and B is the half with of the diffraction peak and θ is the angle. Using the anatase phase (101) peak of TiO₂ is 9.42 nm in diameter approximately.

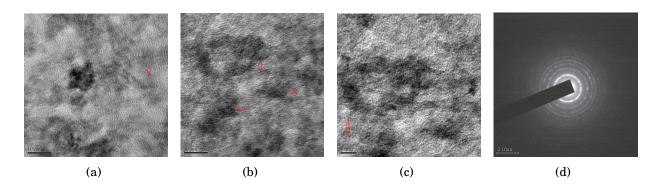


Figure 3. TEM images, and the corresponding SAED pattern of (65 °C) nanocrystalline TiO₂ powder

3.3 TEM analysis of sol-gel prepared crystalline TiO₂ powder

For TEM investigation crystalline TiO₂ powders were the processing temperature in this case was 65 °C. The TEM images (at different magnifications) and the corresponding selected area electron diffraction (SAED) pattern of the TiO₂ samples are shown in Figure 3(a,b,c). Some oval (or spherical) and non-homogeneous structures can be easily seen in figures. The corresponding

SAED pattern (Figure 3(d) consists of sharp and aligned diffraction rings indicating that the TiO₂ nanoparticles are highly crystalline in nature [9]. It is seen that the lattice fringes over an entire oval-shaped TiO₂ particle (marked by an arrow) are uniform in nature. This, in turn, indicates that the individual particle consists of a single grain [9, 11]. Some TEM images of the same sample, at high resolutions, indicate the presence of particles within the size range of 7-10 nm in diameter. Thus, the TEM analysis has confirmed the possibility of existence of a 9.42 nm (in diameter)-sized TiO₂ crystallite as predicted by the XRD (using Scherrer formula). The corresponding SAED pattern Figure 3(d)) shows prominent Debye-Scherrer rings indicating that in this region, the TiO₂ nanoparticles in SiO₂ matrix are crystalline in nature. This indicates that some TiO₂ nanoparticles in the SiO₂ matrix consist of a single grain each, while some others are polycrystalline in nature.

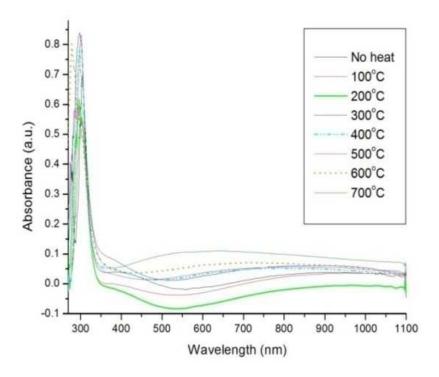


Figure 4. Absorption spectra of TiO₂ film at different temperatures

3.4 Absorption spectra of TiO₂ samples

The absorption spectra of an undoped TiO_2 film annealed at various temperatures are shown in Figure 4. The prepared films were highly transparent and they showed strong absorption in the ultraviolet (UV) region which is a characteristic of nano-sized TiO_2 particles. TiO_2 is an indirect band-gap semiconductor with band-gap energy (E_g) of about $3.1\,\mathrm{eV}$ for pure bulk anatase phase. The absorption edge for the TiO_2 film annealed at $200\,^\circ\mathrm{C}$ lies near about at $330\,\mathrm{nm}$. The corresponding energy of the absorption edge is about $3.761\,\mathrm{eV}$, which is $0.661\,\mathrm{eV}$ higher than that of bulk anatase phase. This temperature is important, since the TiO_2 films showed a maximum "negative absorption" dip near $530\,\mathrm{nm}$ at $200\,^\circ\mathrm{C}$ [6]. Just above to this absorption dip, there is a broad absorption band of the same film annealed at $700\,^\circ\mathrm{C}$.

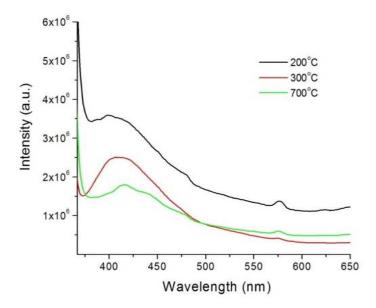


Figure 5. PL spectra of TiO₂ film

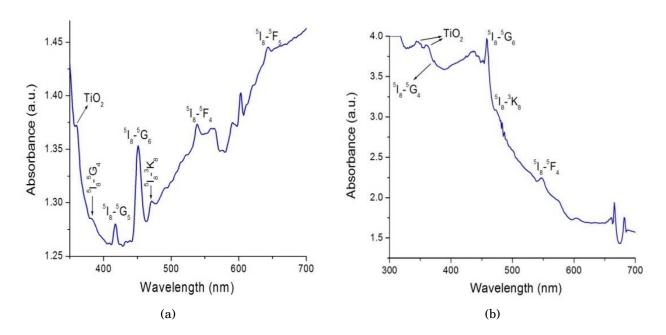


Figure 6. (a) Absorption spectra of $\mathrm{Ho^{3+}}\ 0.1\,\mathrm{ml/20\,ml}\ \mathrm{TIPO}$, (b) Absorption spectra of $\mathrm{Ho^{3+}}\ 0.1\,\mathrm{ml/20\,ml}$ TIPO

This 600 nm absorption band appears because of the formation of defects associated with oxygen vacancies that originate from the reduction of TiO_2 [6] after heat treatment at $700\,^{\circ}$ C. Here, the absorption edge of TiO_2 is at about $332\,\mathrm{nm}$. The corresponding energy of the absorption edge is about $3.738\,\mathrm{eV}$, which is $0.638\,\mathrm{eV}$ higher than that of bulk anatase TiO_2 . The approximate particle size corresponding to the absorption edge can be estimated using the effective mass approximation (EMA) model [10] and is found to be less than 5 nm in diameter.

3.5 Photoluminescence emission and up conversion spectra of undoped TiO₂ film

The photoluminescence (PL) spectra of undoped TiO_2 film recorded under the excitations at 370 nm are shown in Figure 5 respectively. These spectra were taken for three different temperatures, $200\,^{\circ}\text{C}$, $300\,^{\circ}\text{C}$, and $700\,^{\circ}\text{C}$. A broad peak around $400\,\text{nm}$ is observed in the PL emission spectra of the TiO_2 film taken with 370 nm excitation. This $400\,\text{nm}$ peak red-shifts with increase in heating temperature and corresponds to the direct recombination between electrons in the conduction band and holes in the valence band of TiO_2 [9]. The PL intensity is more in the case of the film annealed at $200\,^{\circ}\text{C}$, the temperature at which the TiO_2 film showed a maximum "negative absorption" dip .

3.6 Absorption spectra of Ho3+ doped TiO2-SiO2

Absorption spectra of two $0.05~{\rm Ho^{3+}}$ doped TiO $_2$ -SiO $_2$ gel samples (heated at 65 °C) are shown in Figure 6(a). The sample thickness and refractive index are, $0.6~{\rm cm}$ and 1.887. The concentration of TiO $_2$ precursor, i.e., titanium isopropoxide (TIPO) is $0.1~{\rm ml/20\,ml}$ of the sol from which the gel is formed. In the other sample Figure 6(b) the TIPO concentration is $0.5~{\rm ml/20\,ml}$ of the sol. The assignment of the peaks is shown in Table 1. It is seen that the number of distinct peaks of ${\rm Ho^{3+}}$ decreases with increase in TIPO concentration. The peak corresponding to the transition $^5{\rm I}_5 \rightarrow ^5{\rm G}_5$ almost vanishes in the of (0.5 ml/20 ml) concentration of TIPO. Whereas it is prominent in the sample of $0.1~{\rm ml/20\,ml}$ of TIPO. The absorption bands near 345 and 360 nm can be assigned as due to TiO $_2$. The radiative transitions within the $4f^n$ configuration of a RE ion can be analyzed by the Judd-Ofelt (*J-O*) approach [14, 15]. The *J-O* theory gives an assessment of the oscillator strength characterizing the intensity of a transition between two $^{2S+1}{\rm L}_J$ multiplets within the $4f^n$ configuration of a RE ion [6]. In the frame-work of the *J-O* theory, the theoretical oscillator strength (f_{cal}) is expressed as a sum of transition matrix elements involving the intensity parameters Ω_λ ($\lambda=2,4,6$), which depends on the host matrix and is given by

$$f_{cal}(J,J') = \frac{8\pi^2 mc}{3h\lambda(2J+1)} \frac{(n^2+2)^2}{9n} \sum_{2,4,6} \Omega_{\lambda} \langle aSLJ \| U^{\lambda} \| a'S'L'J' \rangle^2, \tag{3.1}$$

where (2J+1) is the multiplicity of the lower states, λ is the mean wavelength of the transition, c is the velocity of light in vacuum, m is mass of an electron, h is the Planck's constant and n is the measured refractive index. The transition matrix elements $\langle \|U^{\lambda}\| \rangle$ are essentially the same for different hosts. The experimental oscillator strength $f_{\rm exp}$ of the transitions were evaluated from integrating absorbance for each band and the relation is

$$f_{\rm exp} = 4.318 \times 10^{-9} \int \epsilon(\nu) d\nu, \tag{3.2}$$

where $\epsilon(v)$ is the molar extinction coefficient at wave number \overline{v} cm⁻¹. The phenomenological intensity parameters Ω_{λ} for the forced electronic dipole transitions were obtained using MATLAB (MATLAB R12) commands at a suitable step of the calculation within the framework of the *J-O* theory. In this method, three adjacent and prominent peaks in the absorption

spectrum were taken. The reduced matrix elements were used in these calculations. The calculated Judd-Ofelt (*J-O*) intensity parameters Ω_{λ} are summarized in Table 1.

Transition	Energy (cm ⁻¹)	$f_{cal}(\times 10^{-6})$	$f_{cal}(10\times 10^{-6})$
$^{5}I_{8}$ \rightarrow $^{5}F_{5}$	15552	2.464	2.186
${}^{5}I_{8} \rightarrow {}^{5}F_{4} + {}^{5}S_{2}$	18587	3.225	2.958
$^{5}\mathrm{I}_{8}$ \rightarrow $^{5}\mathrm{F}_{3}$	20619	0.808	0.931
$^{5}I_{8} \rightarrow ^{5}F_{2} + ^{3}K_{8}$	21131	0.331	1.172
$^{5}\mathrm{I}_{8}$ \rightarrow $^{5}\mathrm{G}_{6}$	22173	10.396	10.385
$^{5}\mathrm{I}_{8}$ \rightarrow $^{5}\mathrm{G}_{5}$	23981	1.793	1.999

Table 1. Oscillator strengths and J O intensity parameters for HO³⁺:TiO₂-SiO₂ glass

$$\Omega_2 = 1.972 \times 10^{-20} \ cm^2, \quad \Omega_4 = 1.469 \times 10^{-20} \ cm^2, \quad \Omega_6 = 1.227 \times 10^{-20} cm^2$$

The large value of Ω_2 indicate the presence of Ho-O-Ti covalent bond, since it is well established that that the parameter Ω_2 is structure sensitive and associated with the covalency and asymmetry of the RE ion in a particular host.

3.7 PL spectra of Ho doped TiO₂-SiO₂ nanocomposite gel

Figure 7 shows the PL spectra of Ho doped TiO_2 - SiO_2 nanocomposite gel samples under 370 nm excitation the sample revealed strong emission bands near 434 nm, 461 nm and 490 nm (blue). The emission bands at green and red comparatively weak compared to blue bands are also observed at 547 nm and 620 nm In all the samples, the molar RE concentration was kept fixed while varying the TiO_2 -precursor (TIPO) concentration. Some important radiative properties such as spontaneous emission probability (A_R), branching ratio (β_R) for different transitions and radiative life-time (τ_R) of excited states of Ho^{3+} in TiO_2 - SiO_2 nanocomposite gels can be calculated using the value of J-O intensity parameters (Ω^{λ}).

$$A_R(\psi J; \psi' J') = \frac{64\pi v^3 e^2}{3hc^2(2J+1)} \left[\frac{n(n^2+2)^2}{9} S_{ed} + S_{nd} \right], \tag{3.3}$$

where S_{ed} and S_{nd} are electric and magnetic dipole line strengths respectively. The total radiative transition probability (A_R) of an excited state is given shown in Table 2.

Transition	Average energy	A_R	$(\beta_{ m R})$	$(\tau_R)(\mu s)$
$^{5}G_{5} \rightarrow ^{5}I_{8}$	23041	3265	0.482	147.60
$^{5}G_{6} \rightarrow ^{5}I_{8}$	21692	12883	0.860	66.76
5F2→5I2	20408	3321 71	0.816	257 07

Table 2. Calculated radiative parameters for Ho^{3+:}TiO₂-SiO₂ glass

In Table 2, the transitions ${}^5G_5 \rightarrow {}^5I_8$, ${}^5G_5 \rightarrow {}^5I_8$ and ${}^5F_3 \rightarrow {}^5I_8$ accounts for the largest values of radiative properties such as transition probability, branching ratio and life time in the excited state. It is concluded that the aforesaid transition of Ho^{3+} in TiO_2 - SiO_2 glass has the potential to laser transition in the visible region.

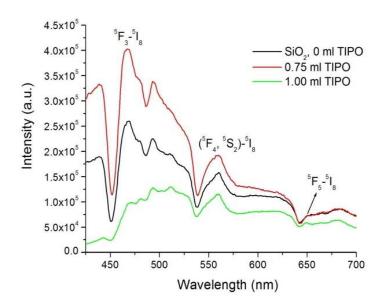


Figure 7. PL spectra of Ho³⁺ with different concentrations of TIPO

It is observed that the characteristics PL intensity of Ho³⁺ in silica xerogel initially increases as the TIPO concentration increases, reaches a maximum, PL intensity observed at 0.75 ml of TIPO. When the concentration of TIOP was further increased, we observed that the emission intensity declined. One possible explanation is that the TiO₂ particle act as network modifiers and increases the concentration of Si dangling and oxygen vacancy in the glass network. In this way, more electrons and holes can be easily excited and radiant recombination's and increased. Moreover, the interesting optical properties of the TiO₂ nanoparticles must be a significant factor. The presence of TiO₂ nanoparticles assist in the excitation of the RE ions by energy transfer from the TiO₂ particles to the RE ions. The decrease in PL with further increase in concentration may be due to the clustering of TiO₂.

3.8 Up Conversion Spectra

Up-conversion spectra of Yb^{3+}/Ho^{3+} is shown in Figure 8(a). It is seen that the up conversion intensity for the Ho^{3+}/Yb^{3+} doped SiO_2 glass sample made with 0.75 ml TIPO (per 20 ml) is much higher than that obtained for the Ho^{3+}/Yb^{3+} -doped SiO_2 glass (1.0 ml TIPO) (per 20 ml). So, TiO_2 - SiO_2 systems can be much better host for RE ions than of simple SiO_2 glasses, provided a suitable RE concentration is used. The upconversion mechanism in Ho^{3+}/Yb^{3+} codoped TiO_2 nanoparticles under 980 nm diode laser excitation as described in Figure 8(b). The Yb^{3+} is initially excited from ground state $^2F_{7/2}$ to $^2F_{5/2}$ via absorbing a 980 nm photon and then transfers it to the Ho^{3+} ion in the ground state via ET process, thereby exciting it to the 5I_6 metastable state. Immediately following this process, subsequent ET from another Yb^{3+} ion

also in the excited state result in the population of the Ho³⁺ in 5F_3 and ${}^5F_4 + {}^5S_2$ state from the metastable ⁵I₆ state through energy transfer (ET)and excited state absorption (ESA) and the excess energy is again dissipated by non radiative process. ESA process ${}^{5}I_{6} \rightarrow {}^{5}F_{4} + {}^{5}S_{2}$ absorption transition of Ho³⁺ is also possible because IR pumping phonon matches quite well with energy gap between the two states. Once the 5F_3 and ${}^5F_4+{}^5S_2$ states are populated, the major part of Ho³⁺ ions returns to the ⁵I₈ ground state. The band near 468 nm (blue) is assigned as due to the ${}^5F_3 \rightarrow {}^5I_8$ optical transition. A distinct Stark-splitting is observed for this transition at 494 nm (blue). The emission band at 560 nm (green) corresponds to the (5F_4 , 5S_2) $\rightarrow {}^5I_8$ transition. A relatively weak band centered on 650 nm (red) is also observed, which is due to the ${}^5F_5 \rightarrow {}^5I_8$ transition. It is observed that the intensity of ${}^5F_3 \rightarrow {}^5I_8$ is the highest among all the other transitions, which is usually not the case for the up conversion spectrum of Ho³⁺ observed in other reported glass host [12,13]. Owing to the large absorption and emission cross section of Yb³⁺ ion is consider to be a preferable sensitizer for catching enough pumping energy and transferring considerable energy to Ho³⁺ ions in TiO₂-SiO₂ glass. The emissions are readily attributed to ET from yb³⁺ to Ho³⁺ ions. The UC intensity of Ho³⁺/Yb³⁺ is approximately 2 times higher than the singly doped Ho³⁺ (not shown in figure) which confirmed that there exists an efficient energy transfer from yb³⁺ to Ho³⁺ ions.

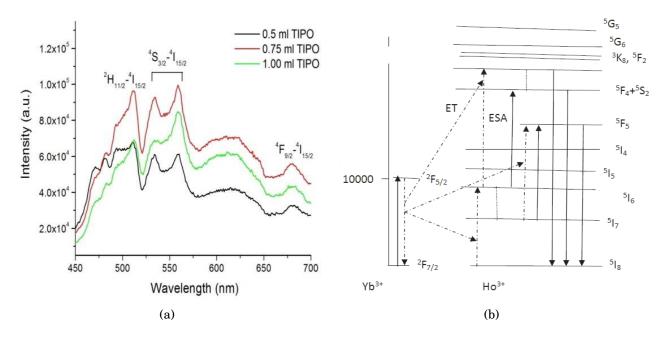


Figure 8. (a) UC spectra of $\mathrm{Ho^{3+}/Yb^{3+}}$ with different concentration of TIPO, (b) Energy level of Yb/Ho presented possible UC

4. Conclusions

The structural and optical properties of $\mathrm{Ho^{3+}}$ in $\mathrm{TiO_2\text{-}SiO_2}$ were studied as a function of active ion concentration. The characteristics emission of $\mathrm{Ho^{3+}}$ was observed in the visible region. We observed the enhanced PL and UC of $\mathrm{Ho^{3+}}$ in $\mathrm{TiO_2}$ nanoparticles embedded in $\mathrm{SiO_2}$ amorphous matrices. By means of optical spectroscopy we observed that fluorescence of $\mathrm{Ho^{3+}}$ doped with

 TiO_2 embedded in SiO_2 amorphous matrices was significantly dependent on concentration of TiO_2 nanoparticles. From the above result we deduce that TiO_2 nanoparticles enter the glass as a network modifier, increase the numbers of non-bridging oxygen in the glass network and weaken the Si-O bonds. This might be of interest for potential applications such as Laser amplifier and optical fiber communication and phosphor materials used in light emitting diodes.

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Competing Interests

The authors declare that he has no competing interests.

Authors' Contributions

Author wrote, read and approved the final manuscript.

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